COMMENTS ON "TOPICS IN ABSOLUTE ANABELIAN GEOMETRY I: GENERALITIES"

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(1.) The final portion [beginning with the *third sentence*] of the statement of Lemma 4.5, (iv), should be replaced by the following text:

> *Then the* **decomposition groups of cusps** $\subseteq H^*$ *may be characterized [*"**group-theoretically**"*] as the* **maximal** *closed subgroups* $I \subseteq H^*$ *isomorphic to* $\mathbb{Z}_l$ *which satisfy the following condition: We have*
>
> $$d_{\chi_G^{\mathrm{cyclo}}}((I^l \cdot J)^{\mathrm{ab}} \otimes \mathbb{Q}_l) + 1 < l \cdot \{d_{\chi_G^{\mathrm{cyclo}}}((I \cdot J)^{\mathrm{ab}} \otimes \mathbb{Q}_l) + 1\}$$
>
> *[i.e., "the covering of curves corresponding to* $J \subseteq I \cdot J$ *is* **totally ramified** *at some cusp"] for every characteristic open subgroup* $J \subseteq H^*$ *such that* $J \neq I \cdot J$.

(2.) In the statement of Proposition 2.5, (iv), the phrase "*Suppose that* k_1 *either an* **FF** *or an* **MLF***;*" should read "*Suppose that* k_1 *is either an* **FF** *or an* **MLF***;*".

(3.) In the final portion of the proof of Proposition 2.5, the phrase "a *MLF*" should read "an *MLF*".

(4.) In Definition 2.9, the phrase "*nonabelian pro-*Σ*-solvable free group*" should be replaced by the phrase "*nonabelian free pro-*Σ*-solvable group* [cf. [FJ], Definition 17.4.1]".

(5.) In the statement and (second paragraph of) the proof of Theorem 2.11, (iv), the notation "ϕ" should be replaced by the phrase "the natural inclusion $H \hookrightarrow J$".

(6.) In the proof of Proposition 3.2, the phrase "follows immediately the Hodge-Tate" should be replaced by the phrase "follows immediately from the Hodge-Tate".

(7.) In Remark 3.7.1, the phrase "continue to hold when" should be replaced by the text "continue to hold, at least under the additional assumption that each field k_i contains a primitive p-th root of unity, when".

(8.) In the final portion of the second line of the display in the statement of Proposition A.3, (ix), the notation "v_j" should be replaced by "$\phi_V(v_j)$".

(9.) In the third sentence of the proof of Proposition A.6, (ii), the notation "$W \times_S k$" should be replaced by "$W \times_k S$".